

# Root findings : equations $f(x) = 0$



Algorithm used to find roots of an equation use iterations, and a numerical criterion to accept a solution when a sufficiently accurate value is reached. The rate of convergence depends on the used method and the function  $f(x)$ . Some methods (Newton-Raphson) need the derivative of the function  $f(x)$ .

- Polynomial equations : [W Bairstow's method](#) is an efficient algorithm for finding the roots of a real polynomial of arbitrary degree
  - [Polynomials in NumPy](#)
  - [polynomial module](#), including `polyroots` to compute the roots of a polynomial.
- [W Bisection method](#) (dichotomy) : very simple and robust method, but relatively slow. It assumes continuity of the function, and obtain one roots. The algorithm is based on a [W loop invariant](#) property : an interval  $[a, b]$  is said to bracket a root if  $f(a)$  and  $f(b)$  have opposite signs.
- [W Secant method](#) (retains the last two computed points)
- [W Regula falsi](#) (retains the points which preserve bracketing)
- [W Newton-Raphson method](#)
- Chapter 9 in the book "Numerical Recipes" : Root finding an nonlinear sets of equations
  - 9.0 Introduction
  - 9.1 Bracketing and Bisection
  - 9.2 Secant Method, False Position Method, and Ridders' Method
  - 9.4 Newton-Raphson Method Using Derivative
  - 9.5 Roots of Polynomials
- Python [NumPy](#) library : [SciPy Reference](#)
  - [scipy.optimize](#) package (root)

## Applications

- ...

## Références

- Numerical recipes, The Art of Scientific Computing 3rd Edition, William H. Press, Saul A. Teukolsky, William T. Vetterling, Brian P. Flannery, 2007, isbn: 9780521880688
  - <http://numerical.recipes/>
    - in C : <http://apps.nrbook.com/c/index.html>
  - [http://www2.units.it/ipi/students\\_area/imm2/files/Numerical\\_Recipes.pdf](http://www2.units.it/ipi/students_area/imm2/files/Numerical_Recipes.pdf), p 347...
  - <http://apps.nrbook.com/empanel/index.html#>
    - Chapter 9 : Root finding an nonlinear sets of equations

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